

# Dividing Polynomials Worksheet Answer Key PDF

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## Part 1: Building a Foundation

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**What is the definition of a polynomial?**

undefined. A) An expression with variables and coefficients, involving only addition and subtraction.

undefined. **B) An expression with variables and coefficients, involving addition, subtraction, multiplication, and non-negative integer exponents.** ✓

undefined. C) An expression with variables and coefficients, involving only multiplication and division.

undefined. D) An expression with variables and coefficients, involving only non-negative integer exponents.

A polynomial is an expression that includes variables and coefficients, with operations of addition, subtraction, multiplication, and non-negative integer exponents.

**Which of the following are methods for dividing polynomials?**

undefined. **A) Long Division** ✓

undefined. **B) Synthetic Division** ✓

undefined. C) Matrix Division

undefined. D) Factorization

The methods for dividing polynomials include Long Division and Synthetic Division.

**Explain the Remainder Theorem in your own words.**

**The Remainder Theorem states that when a polynomial is divided by a linear divisor, the remainder is equal to the value of the polynomial evaluated at the root of the divisor.**

**List the steps involved in polynomial long division.**

1. Step 1

**Divide the leading term of the dividend by the leading term of the divisor.**

2. Step 2

**Multiply the entire divisor by the result from Step 1.**

3. Step 3

**Subtract the result from the dividend.**

4. Step 4

**Bring down the next term from the dividend.**

5. Step 5

**Repeat the process until the remainder is of lower degree than the divisor.**

The steps include dividing the leading term, multiplying, subtractively combining, and repeating until the remainder is of lower degree than the divisor.

**What is the form of a divisor suitable for synthetic division?**

undefined. A)  $x^2 + bx + c$

**undefined. B)  $x - c$  ✓**

undefined. C)  $ax + b$

undefined. D)  $x^3 + bx^2 + cx + d$

The suitable form for synthetic division is a linear divisor of the form  $x - c$ .

## Part 2: Understanding and Application

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**What does the Factor Theorem state about a polynomial  $f(x)$  and a factor  $x - c$ ?**

**undefined. A)  $f(c) = 0$  implies  $x - c$  is a factor of  $f(x)$ . ✓**

undefined. B)  $f(c) \neq 0$  implies  $x - c$  is a factor of  $f(x)$ .

undefined. C)  $f(c) = 0$  implies  $x + c$  is a factor of  $f(x)$ .

undefined. D)  $f(c) \neq 0$  implies  $x + c$  is a factor of  $f(x)$ .

The Factor Theorem states that if  $f(c) = 0$ , then  $x - c$  is a factor of the polynomial  $f(x)$ .

**Which statements are true about polynomial division?**

undefined. A) The quotient is always a polynomial of lower degree than the dividend.

undefined. B) The remainder is always a constant.

**undefined. C) The remainder can be a polynomial of lower degree than the divisor. ✓**

undefined. **D) The division process stops when the degree of the remainder is less than the degree of the divisor.** ✓

The true statements include that the division process stops when the degree of the remainder is less than the degree of the divisor.

**Describe how synthetic division simplifies the division process compared to long division.**

**Synthetic division simplifies the process by using only the coefficients of the polynomial and requires fewer steps than long division.**

**Perform the long division of  $2x^3 + 3x^2 - 5x + 6$  by  $x - 2$  and provide the quotient and remainder.**

**The quotient is  $2x^2 + 7$  and the remainder is 20.**

**Using synthetic division, divide  $x^3 - 6x^2 + 11x - 6$  by  $x - 3$ . List the quotient and remainder.**

1. Quotient

**$x^2 - 3x + 2$**

2. Remainder

**0**

The quotient is  $x^2 - 3x + 2$  and the remainder is 0.

**If  $f(x) = x^2 - 4x + 4$ , what is the remainder when  $f(x)$  is divided by  $x - 2$ ?**

undefined. **A) 0** ✓

undefined. B) 2

undefined. C) 4

undefined. D) -2

The remainder is 0, indicating that  $x - 2$  is a factor of  $f(x)$ .

### Part 3: Analysis, Evaluation, and Creation

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**Analyze the relationship between the Remainder Theorem and the Factor Theorem. How do they complement each other in polynomial division?**

The Remainder Theorem provides a way to find the remainder of a polynomial division, while the Factor Theorem helps identify factors based on the remainder being zero.

Which of the following statements correctly describe the outcomes of polynomial division?

undefined. A) The degree of the quotient is always one less than the degree of the dividend.

undefined. B) The remainder can be zero, indicating the divisor is a factor of the dividend. ✓

undefined. C) If the remainder is non-zero, the divisor is not a factor of the dividend. ✓

undefined. D) The degree of the remainder is always less than the degree of the divisor. ✓

The correct statements include that the remainder can be zero, indicating the divisor is a factor of the dividend.

Given  $f(x) = x^3 - 7x + 6$ , determine if  $x - 1$  is a factor of  $f(x)$ .

undefined. A) Yes, because  $f(1) = 0$ . ✓

undefined. B) No, because  $f(1) \neq 0$ .

undefined. C) Yes, because  $f(-1) = 0$ .

undefined. D) No, because  $f(-1) \neq 0$ .

$x - 1$  is a factor of  $f(x)$  because  $f(1) = 0$ .

Evaluate the effectiveness of using synthetic division over long division in solving polynomial division problems. Discuss scenarios where one method might be preferred over the other.

Synthetic division is often more efficient for linear divisors, while long division is necessary for higher degree divisors.

Create a polynomial  $g(x)$  such that when divided by  $x - 3$ , the remainder is 5. Provide the polynomial and explain your reasoning.

1. Polynomial

$$g(x) = (x - 3)(x + 2) + 5$$

2. Reason

The polynomial is constructed to ensure the remainder is 5 when divided by  $x - 3$ .

A polynomial such as  $g(x) = (x - 3)(x + 2) + 5$  will have a remainder of 5 when divided by  $x - 3$ .

**Which of the following best describes a scenario where the Remainder Theorem is particularly useful?**

undefined. **A) When checking if a polynomial is divisible by a linear factor. ✓**

undefined. B) When finding the exact quotient of a polynomial division.

undefined. C) When simplifying a polynomial expression.

undefined. D) When determining the degree of a polynomial.

The Remainder Theorem is particularly useful when checking if a polynomial is divisible by a linear factor.